

## Difference Equations on the TI 82

The TI 82 can easily be used to define difference equations and to view the results graphically and numerically.

### Quick Recursive Calculation

The TI 82 is programmed to repeat the preceding computation if the **ENTER** key is pressed repeatedly. This can be used to do recursion by arranging that the result of the preceding calculation appears as **ANS** in the command line. Try this example: start by keying in 100 and hitting **ENTER**. (That makes 100 the value in the **ANS** memory.) Next key in:  $\times .2 + 60$  **ENTER**. Now keep hitting the **ENTER** key 4 or 5 times. Each time you hit **ENTER**, the calculator is computing  $\text{ANS} * .2 + 60$ . That is, the calculator is computing terms according to the difference equation  $a_{n+1} = .2a_n + 60$ . In a similar way, any difference equation of the form  $a_{n+1} = f(a_n)$  can be computed. First key in  $a_0$  and **ENTER**. Then key in the computation of  $f$ , using the **ANS** key each time you need to enter the variable for  $f$ . Thereafter, each time you hit **ENTER**, the calculator will apply  $f$  to the preceding result.

### Mode Settings

Put the calculator into sequential mode as follows: push the **MODE** key, use the down arrow to get to the row starting with **FUNC**, then use the right arrow to get to **SEQ**, and hit **ENTER**. Then go down to the next line and over to **DOT**, and hit **ENTER** again. This will make graphs come up as discrete points. The combination **2ND QUIT** will return the calculator to its normal appearance.

### Defining An Equation

Hit the button labeled **Y=**. You should see two lines, one for defining  $u_n$  and the other for  $v_n$ . You can enter an expression on the other side of the equal sign that is either an explicit function of  $n$ , or is recursive (depending on  $u_{n-1}$ ). Notice that  $u_{n-1}$ ,  $v_{n-1}$ , and  $n$  are available as **2ND** key choices above the **7**, **8**, and **9** keys.

### Graph Setting

Next hit the **WINDOW** key, to assign initial values for  $n$ ,  $u_n$ , and  $v_n$  (if you are using  $v_n$ ), as well as the min and max  $x$  and  $y$  values for the graph. After making these entries, hit the **GRAPH** button to see the graph of your sequence or sequences.

### Table Settings

The combination **2ND TBLSET** brings up a menu for creating a table of sequence entries. The **TBLMIN** variable is the first  $n$  value for the table; the  $\Delta$ **TBL** variable specifies the step size between table entries for  $n$ . Once those are set, if you use **2ND TABLE** you will see a table of sequence values for  $u_n$  (and  $v_n$ , if defined). This table is scrollable using the up and down arrow keys.